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On the non-separable descriptive theory

Z.Frolík, P.Holický

The theory of analytic spaces or sets is extended to a wider class of spaces containing also some non-Lindelöf spaces, particularly all complete metric spaces and their products with compact spaces. In the hyperanalytic spaces defined below the technique of upper semi-continuous compact-valued mappings, and also the technique used in non-separable metric spaces can be used. Definition 2 therefore enables to study the descriptive theory in non-separable spaces like an extension of the separable theory which was studied separately till now.

Definition 1. Say that a family $\{X_a\}_{a \in A}$ is σ -d.d. (σ -discretely descomposable) in the uniform space X if there are sets X_{an} , $a \in A$, and $n \in \omega$, such that $X_a = \bigcup_{n \in \omega} X_{an}$, and the families $\{X_{an}\}_{a \in A}$ are discrete.

Definition 2. Say that the uniform space H is hyperanalytic if there are a complete metric space M , and an upper semi-continuous compact-valued mapping f from M onto H , such that images of σ -d. d. families in M are σ -d.d. in H .

The hyperanalytic spaces have a lot of very special properties, for example they are paracompact and absolutely Souslin in some sense. We describe the strongest properties in Theorems 1 and 2.

Theorem 1. Let $\{X_a\}$ be a point-finite completely hyperanalytic-additive family of sets (subspaces) of the uniform space X (e.g. every subunion of $\langle X_a \rangle$ is hyperanalytic in X). Then, $\langle X_a \rangle$ is σ -d.d. in X .

Theorem 2. Let H be hyperanalytic, and S Souslin subsets of the uniform space X . If $H \cap S = \emptyset$, then there is a hyper-Baire set B

in X , such that $H \subset B \subset X-S$.

Remark. The ideas of the described theory follows Hansell's ideas for complete metric spaces, and the technique of upper semi-continuous compact-valued mappings introduced by the first author.

The properties of hyperanalytic spaces, proofs of Theorems 1 and 2, and further theorems will be published elsewhere.