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On descriptive classification of set-functors. II.

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ON DESCRIPTIVE CLASSIFICATION OF SET-FUNCTORS II.

Věra TRNKOVÁ, Praha

The present paper is a continuation of [1]. In [1] the preservation of limits of various types of diagrams by set-functors is studied. Here, the dual questions, concerning coequalizers, push-out-diagrams, colimits up to  $\aleph_n$  are investigated. The paper has three parts, numbered IX. to XI. In IX, the coequalizer-preserving set-functors are characterized. In X, the preservation of push-out-diagrams and colimits up to  $\aleph_n$  is considered. We prove, for example, that every set-functor which preserves colimits of finite diagrams, preserves also colimits of countable diagrams. In XI, the set-functors preserving some types of limits and some types of colimits are investigated. For example, the functors that preserve pull-back-push-out diagrams are characterized.

The notation, all the conventions and some facts from [1] are used.

IX.

IX.1. Definition. Let  $H$  be a functor,  $f, g: X \rightarrow Y$  mappings,  $\psi_1, \psi_2 \in H(Y)$ . An  $m$ -tuple

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$\langle \langle \rho_1, x_1, t_1 \rangle, \dots, \langle \rho_m, x_m, t_m \rangle \rangle$  will be called an  $(f, g)$ -chain from  $\psi_1$  to  $\psi_2$  in  $H$  iff

- 1)  $\{\rho_i, t_i\} = \{f, g\}$  for  $i = 1, \dots, m$  ;
- 2)  $x_1, \dots, x_m \in H(X)$  ;
- 3)  $[H(\rho_1)](x_1) = \psi_1$  ,  $[H(t_m)](x_m) = \psi_2$  ;
- 4)  $[H(t_i)](x_i) = [H(\rho_{i+1})](x_{i+1})$  for  $i = 1, \dots, m - 1$  .

IX.2. Proposition. If  $\mathcal{F}$  is a  $\mathcal{K}_1$ -complete ultrafilter on a set  $M$  , then  $\mathcal{Q}_{M, \mathcal{F}}$  preserves coequalizers.

Proof. Put  $H = \mathcal{Q}_{M, \mathcal{F}}$  . Let  $f, g: X \rightarrow Y$  be mappings,  $h = \text{coeq}(f, g)$  . We prove that  $H(h) = \text{coeq}(H(f), H(g))$  . Let  $\kappa_1^+, \kappa_2^+ \in H(Y)$  ,  $[H(h)](\kappa_1^+) = [H(h)](\kappa_2^+)$  . Then there exists an  $F_0 \in \mathcal{F}$  such that  $h \circ \kappa_1(x) = h \circ \kappa_2(x)$  for every  $x \in F_0$  . Consequently one can choose an  $(f, g)$ -chain  $\mu^x = \langle \langle \rho_1^x, x_1^x, t_1^x \rangle, \dots, \langle \rho_{m_x}^x, x_{m_x}^x, t_{m_x}^x \rangle \rangle$  from  $\kappa_1(x)$  to  $\kappa_2(x)$  in  $I$  . Define an equivalence  $\sim$  on  $F_0$  by

$$\begin{aligned} x \sim x' &\iff \langle \langle \rho_1^x, t_1^x \rangle, \dots, \langle \rho_{m_x}^x, t_{m_x}^x \rangle \rangle = \\ &= \langle \langle \rho_1^{x'}, t_1^{x'} \rangle, \dots, \langle \rho_{m_{x'}}^{x'}, t_{m_{x'}}^{x'} \rangle \rangle . \end{aligned}$$

The decomposition of  $F_0$  by means of  $\sim$  is countable; let  $A$  be its element which is in  $\mathcal{F}$  . If  $\alpha_i: M \rightarrow X$  are mappings such that  $\alpha_i(x) = x_i^x$  for all  $x \in A$  , then obviously  $\langle \langle \rho_1^x, \alpha_1^+, t_1^x \rangle, \dots, \langle \rho_{m_x}^x, \alpha_{m_x}^+, t_{m_x}^x \rangle \rangle$

is an  $(f, g)$ -chain from  $\kappa_1^+$  to  $\kappa_2^+$  in  $H$  for any  $z \in A$ .

**IX.3. Proposition.** A factorfunctor of a coequalizer-preserving functor preserves coequalizers.

**Proof.** Let  $\gamma : H \rightarrow G$  be an epitransformation. Let  $H$  preserve coequalizers,  $f, g : X \rightarrow Y$  be mappings,  $h = \text{coeq}(f, g)$ ,  $h : Y \rightarrow Z$ . Let  $y, y' \in G(Y)$ ,  $[G(h)](y) = [G(h)](y')$ . We prove that there exists an  $(f, g)$ -chain from  $y$  to  $y'$  in  $G$ . Choose  $x, x' \in H(Y)$  with  $\gamma_y(x) = y$ ,  $\gamma_y(x') = y'$ . Let  $[H(h)](x) = b'$ ,  $[H(h)](x') = b''$ . Then  $\gamma_z(b') = a = \gamma_z(b'')$ . Choose  $l : Z \rightarrow Y$  with  $h \circ l = \text{id}_Z$  and put  $c = [H(l)](b')$ ,  $c' = [H(l)](b'')$ . Since  $[H(h)](x) = b' = [H(h)](c)$ , there is an  $(f, g)$ -chain  $\langle \langle s_1, x_1, t_1 \rangle, \dots, \langle s_m, x_m, t_m \rangle \rangle$  from  $x$  to  $c$  in  $H$ . Analogously, there exists an  $(f, g)$ -chain  $\langle \langle s'_1, x'_1, t'_1 \rangle, \dots, \langle s'_m, x'_m, t'_m \rangle \rangle$  from  $c'$  to  $x'$  in  $H$ . Since  $\gamma_y(c) = [G(l)](a) = \gamma_y(c')$ ,  $\langle \langle s_1, \gamma_x(x_1), t_1 \rangle, \dots, \langle s_m, \gamma_x(x_m), t_m \rangle, \langle s'_1, \gamma_x(x'_1), t'_1 \rangle, \dots, \langle s'_m, \gamma_x(x'_m), t'_m \rangle \rangle$  is an  $(f, g)$ -chain from  $y$  to  $y'$  in  $G$ .

**IX.4. Definition.** Let  $\mu$  be an infinite cardinal. We recall that a functor  $H$  preserves unions up to  $\mu$  iff

$$H(X) = \bigcup_{\alpha \in A} H(X_\alpha)_X \quad \text{whenever } X = \bigcup_{\alpha \in A} X_\alpha \text{ and}$$

$\text{card } A < \mu$ .

IX.5. Lemma. Let  $\mathfrak{m}$  be an infinite cardinal, let  $H$  be a functor such that

if  $\{X_\alpha; \alpha \in A\}$  is a disjoint collection such that  $\text{card } A < \mathfrak{m}$  and  $\text{card } X_\alpha = \text{card } X_\alpha$ , for every  $\alpha, \alpha'$ , then  $H(X) = \bigcup_{\alpha \in A} H(X_\alpha)_X$  where  $X = \bigcup_{\alpha \in A} X_\alpha$ .

Then  $H$  preserves unions up to  $\mathfrak{m}$ .

Proof. 1) Let  $\{Y_\alpha; \alpha \in A\}$  be a disjoint collection of non-empty sets,  $\text{card } A < \mathfrak{m}$ . Choose a disjoint collection  $\{X_\alpha; \alpha \in A\}$  such that  $Y_\alpha \subset X_\alpha$  and  $\text{card } X_\alpha = \sup_{\beta \in A} \text{card } Y_\beta$  for all  $\alpha \in A$ . Put  $X = \bigcup_{\alpha \in A} X_\alpha$ ,  $Y = \bigcup_{\alpha \in A} Y_\alpha$ . Then  $H(X) = \bigcup_{\alpha \in A} H(X_\alpha)_X$ . Since  $Y_\alpha \neq \emptyset$ ,  $Y_\alpha = X_\alpha \cap Y$ , we have  $H(Y_\alpha)_X = H(Y)_X \cap H(X_\alpha)_X$ . Consequently  $H(Y)_X = H(Y)_X \cap H(X) = H(Y)_X \cap \left( \bigcup_{\alpha \in A} H(X_\alpha)_X \right) = \bigcup_{\alpha \in A} H(Y_\alpha)_X$ .

Thus,  $H(Y) = \bigcup_{\alpha \in A} H(Y_\alpha)_Y$ .

2) Let  $\{Y_\alpha; \alpha \in A\}$  be a disjoint collection,  $\text{card } A < \mathfrak{m}$ ,  $Y = \bigcup_{\alpha \in A} Y_\alpha$ . If all  $Y_\alpha$  are empty, then  $Y = \emptyset$  and then  $H(Y) = \bigcup_{\alpha \in A} H(Y_\alpha)_Y$ . If  $B = \{\alpha \in A; Y_\alpha \neq \emptyset\} \neq \emptyset$ , then  $Y = \bigcup_{\alpha \in B} Y_\alpha$  and  $H(Y) = \bigcup_{\alpha \in B} H(Y_\alpha)_Y = \bigcup_{\alpha \in A} H(Y_\alpha)_Y$ .

3) If  $\{Y_\alpha; \alpha \in A\}$  is an arbitrary collection with  $\text{card } A < \mathfrak{m}$ , take a well-ordering  $<$  of  $A$  and put  $Z_\alpha = Y_\alpha - \bigcup_{\beta < \alpha} Y_\beta$ . Then

$Y = \bigcup_{\alpha \in A} Y_\alpha = \bigcup_{\alpha \in A} Z_\alpha$  and consequently  
 $H(Y) = \bigcup_{\alpha \in A} H(Z_\alpha)_Y$ . Since  $H(Z_\alpha)_Y \subset H(Y_\alpha)_Y \subset H(Y)$ , we have  $H(Y) = \bigcup_{\alpha \in A} H(Y_\alpha)_Y$ .

IX.6. Lemma. Let  $\mathfrak{m}$  be an infinite cardinal. A functor  $H$  preserves unions up to  $\mathfrak{m}$  iff for every set  $X$  and every  $x \in H(X)$  either the pair  $\langle x, X \rangle$  is distinguished or  $H^{x, X}$  is an  $\mathfrak{m}$ -complete ultrafilter.

Proof. 1) Let  $H$  preserve unions up to  $\mathfrak{m}$ , let  $x \in H(X)$ ,  $\langle x, X \rangle$  be not distinguished. Let  $\{X_\alpha; \alpha \in A\}$  be a decomposition of  $X$ ,  $\text{card } A < \mathfrak{m}$ . Since  $x \in H(X_{\alpha_0})_X$  for some  $\alpha_0 \in A$ , we have  $X_{\alpha_0} \in H^{x, X}$ .

2) Let  $H^{x, X}$  be an  $\mathfrak{m}$ -complete ultrafilter whenever  $\langle x, X \rangle$  is not distinguished. Let  $X = \bigcup_{\alpha \in A} X_\alpha$ ,  $\text{card } A < \mathfrak{m}$ . If  $X = \emptyset$ , then necessarily  $H(X) = \bigcup_{\alpha \in A} H(X_\alpha)_X$ . If  $X \neq \emptyset$ , then there exists an  $\alpha_0 \in A$  such that  $X_{\alpha_0} \neq \emptyset$ . Then  $x \in H(X_{\alpha_0})_X$  whenever  $\langle x, X \rangle$  is distinguished. If  $\langle x, X \rangle$  is not distinguished then  $X_{\alpha_1} \in H^{x, X}$  for some  $\alpha_1 \in A$ . Thus,  $H(X) = \bigcup_{\alpha \in A} H(X_\alpha)_X$ .

IX.7. Lemma. Let  $H$  preserve coequalizers of all pairs of bijections. Then it preserves countable unions.

Proof. Let  $\mathbb{Z}$  be the set of all integers. It is sufficient to prove (see IX.5) that  $H$  preserves unions of all disjoint collections  $\{X_m; m \in \mathbb{Z}\}$ , where

all  $X_m$  have the same cardinality. Put  $X = \bigcup_{m \in \mathbb{Z}} X_m$  and denote by  $i_m : X_m \rightarrow X$  the inclusion. For every  $m \in \mathbb{Z}$  choose a bijection  $g_m : X_m \rightarrow X_{m+1}$ . Let  $g : X \rightarrow X$  be the mapping with  $g \circ i_m = i_{m+1} \circ g_m$  for all  $m \in \mathbb{Z}$ . Put  $T = \bigcup_{m \in \mathbb{Z}} H(X_m)_X$ . Then

(\*)  $[H(g)](T) \subset T, [H(g)]^{-1} \subset T$ .

Let  $\alpha = \text{coeq}(id_X, g)$ . We may suppose  $\alpha : X \rightarrow X_0, \alpha \circ i_0 = id_{X_0}$ . Let  $x \in H(X)$ . Put  $c = [H(i_0 \circ \alpha)](x)$ , then  $[H(\alpha)](x) = [H(\alpha)](c)$ .

Consequently there exists an  $(id_X, g)$ -chain from  $x$  to  $c$  in  $H$ . Then necessarily either  $c = [H(g)]^k(x)$  for some natural  $k$ , or  $x = [H(g)]^l(c)$  for some natural  $l$ . Since  $c \in T$ , (\*) implies  $x \in T$ .

**IX.8. Theorem.** The following properties of a functor  $H$  are equivalent:

- (i)  $H$  preserves coequalizers;
- (ii)  $H$  preserves coequalizers of pairs of bijections;
- (iii)  $H$  preserves countable unions;
- (iv) for every set  $X$  and every  $x \in H(X)$  either the pair  $\langle x, X \rangle$  is distinguished or  $H^{x, X}$  is a  $\mathcal{K}_1$ -complete ultrafilter.

**Proof.** (i)  $\implies$  (ii) is trivial, for (ii)  $\implies$  (iii) see IX.7, for (iii)  $\implies$  (iv) see IX.6.

(iv)  $\implies$  (i): Let  $H$  do not preserve coequalizers. Then there are  $f, g : X \rightarrow Y$  and  $\alpha, \beta \in H(Y)$  such that  $[H(\alpha)](\alpha) = [H(\alpha)](\beta)$ , where

$\alpha = \text{coeq}_2(f, g)$ , while there is no  $(f, g)$ -chain from  $a$  to  $b$  in  $H$ . Put  $G = H_{\langle a, Y \rangle} \cup H_{\langle b, Y \rangle}$ . Then  $G$  does not preserve coequalizers. Put  $K_a = H_{\langle a, Y \rangle}$  if  $\langle a, Y \rangle$  is distinguished,  $K_a = Q_{Y, H^a, Y}$  otherwise. Put  $K_b = H_{\langle b, Y \rangle}$  if  $\langle b, Y \rangle$  is distinguished,  $K_b = Q_{Y, H^b, Y}$  otherwise. Since  $G$  is a factorfunctor of  $K_a \vee K_b$ , either  $K_a$  or  $K_b$  does not preserve coequalizers (see IX.3). If  $K_a$  does not preserve coequalizers then  $\langle a, Y \rangle$  is not distinguished and  $H^{a, Y}$  is not an  $\mathcal{S}_1$ -complete ultrafilter (see IX.2)

**Corollary.** Every subfunctor of a coequalizer-preserving functor preserves coequalizers.

## X.

**X.1. Convention.** Denote by  $\mathcal{P}$  the category of all pointed sets, i.e.  $\mathcal{P}^\sigma$  is the class of all  $\langle A, a \rangle$ , where  $A$  is a set and  $a \in A$ ;  $f : \langle A, a \rangle \rightarrow \langle B, b \rangle$  is a morphism of  $\mathcal{P}$  iff it is a mapping  $f : A \rightarrow B$  with  $f(a) = b$ . Denote by  $\square : \mathcal{P} \rightarrow \mathcal{S}$  the obvious forgetful-functor.

**X.2. Lemma.** In the category  $\mathcal{P}$  every diagram has a colimit and the functor  $\square : \mathcal{P} \rightarrow \mathcal{S}$  preserves coequalizers and push-out-diagrams.

**Proof** is trivial.

**X.3. Lemma.** Let  $H : \mathcal{S} \rightarrow \mathcal{S}$  be a connected functor with  $\text{card } H(\emptyset) = 1$ . Then there exists exactly one  $\bar{H} : \mathcal{S} \rightarrow \mathcal{P}$  with  $\square \circ \bar{H} = H$

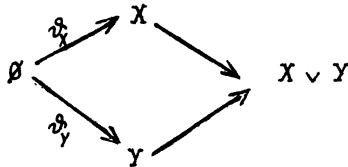


Proof: It is evident.

Convention. If  $H : \mathcal{S} \rightarrow \mathcal{S}$  is a connected functor with  $\text{card } H(\emptyset) = 1$ , then  $\bar{H}$  always denotes the functor from the lemma.

X.4. Lemma. Let  $H : \mathcal{S} \rightarrow \mathcal{S}$  be a connected functor with  $\text{card } H(\emptyset) = 1$ . If  $H$  preserves coequalizers or push-out-diagrams, then  $\bar{H}$  preserves colimits of finite diagrams.

Proof. If  $H$  preserves coequalizers or push-out-diagrams, then  $\bar{H}$  also preserves them. Consequently it is sufficient to prove that  $\bar{H}$  preserves finite sums. If  $H$  preserves coequalizers, this follows from IX.7. If  $H$  preserves push-out-diagrams, use the diagram



X.5. Proposition. The following properties of a functor  $H$  are equivalent:

- (i)  $H$  preserves push-out-diagrams;
- (ii)  $H$  is regular and preserves coequalizers.

Proof. We may suppose  $H$  connected.

(i)  $\implies$  (ii): If  $H$  preserves push-out-diagrams, it is regular, clearly. If  $H(\emptyset) = \emptyset$ , then  $H$  preserves finite sums, consequently it preserves finite colimits, in particular coequalizers. If  $H(\emptyset) \neq \emptyset$ , consider a functor  $G$  with  $G^* = H^*$ ,  $\text{card } G(\emptyset) = 1$  and use X.4, X.2 for  $\bar{G}$ . Then  $\bar{G}$  preserves coequalizers and so does  $H$ .

(ii)  $\implies$  (i): If  $H(\emptyset) = \emptyset$ , then  $H$  preserves finite sums (see IX.8 and II.4 in [1]), consequently it preserves finite colimits, in particular push-out-diagrams. If  $H(\emptyset) \neq \emptyset$ , consider a functor  $G$  with  $G^* = H^*$ , and  $G(\emptyset) = 1$  and use X.4, X.2 again.

Corollary. Every regular subfunctor of a push-out-diagram-preserving functor preserves push-out-diagrams.

X.6. Theorem. The following properties of a functor  $H$  are equivalent:

- (i)  $H$  preserves colimits of countable diagrams;
- (ii)  $H$  preserves colimits of finite diagrams;
- (iii)  $H$  is separating and preserves push-out-diagrams;
- (iv)  $H$  is separating and preserves coequalizers of pairs of bijections;
- (v)  $H$  is separating and for every  $x \in H(X)$  the filter  $H^{x, X}$  is an  $\mathcal{K}_1$ -complete ultrafilter;
- (vi)  $H$  preserves countable sums.

Proof. The implications (i)  $\implies$  (ii), (ii)  $\implies$  (iii) are trivial. (iii)  $\iff$  (iv) follows from X.5 and IX.8, (iv)  $\iff$  (v) follows from IX.8, (v)  $\implies$  (vi) is easy. Clearly, ((vi) and (iii))  $\implies$  (i).

X.7. Theorem. Let  $\mathcal{M} > \mathcal{K}_0$ . The following properties of a functor  $H$  are equivalent:

- (i)  $H$  preserves colimits of diagrams up to  $\mathcal{M}$ ;
- (ii)  $H$  preserves sums up to  $\mathcal{M}$ ;
- (iii)  $H$  is separating and for every  $x \in H(X)$  the filter  $H^{x, X}$  is an  $\mathcal{M}$ -complete ultrafilter.

Proof is analogous to the previous one.

Corollary. Every subfunctor of a functor which preserves colimits of diagrams up to  $\mathcal{M}$  also preserves colimits up to  $\mathcal{M}$ .

X.8. Theorem. Every one from the following assertions is equivalent to the non-existence of measurable cardinal:

- (1) The functors preserving colimits of finite diagrams are precisely  $\cong I \times C_M$ .
- (2) The functors preserving push-put-diagrams are precisely  $\cong (I \times C_M) \vee C_{T, t, L}$ , where  $t: T \rightarrow L$  is a surjection.
- (3) The functors preserving coequalizers are precisely  $\cong (I \times C_M) \vee C_{T, t, L}$ .

Proof follows easily from X.6, X.5 and IX.8.

## XI.

XI.1. Theorem. Every one of the following assertions is equivalent to the non-existence of a measurable cardinal:

- (1) If a functor  $H$  preserves finite sums and countable products then either  $H = C_0$  or  $H \cong I$ .
- (2) If a functor  $H$  preserves countable sums and finite products then either  $H = C_0$  or  $H \cong I$ .
- (3) If a functor  $H$  preserves limits of finite diagrams and colimits of finite diagrams then either  $H = C_0$  or  $H \cong I$ .

Proof follows easily from X.8.

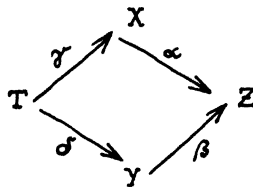
XI.2. Proposition. If a functor preserves finite sums then it preserves proimages and sets of fixed points.

Proof. If a functor  $H$  preserves finite sums, then

it is separating and  $H^{\alpha, X}$  is an ultrafilter for every  $X$ ,  $\alpha \in H(X)$ . The mappings  $\mathcal{G}_X : H(X) \rightarrow \beta(X)$  with  $\mathcal{G}_X(\alpha) = H^{\alpha, X}$  form a natural transformation. Consequently  $H$  preserves proimages. Since  $\beta$  preserves sets of fixed points (see VI.8) one can prove easily that  $H$  preserves sets of fixed points.

XI.3. We recall that a pull-back-push-out diagram is called a double-diagram.

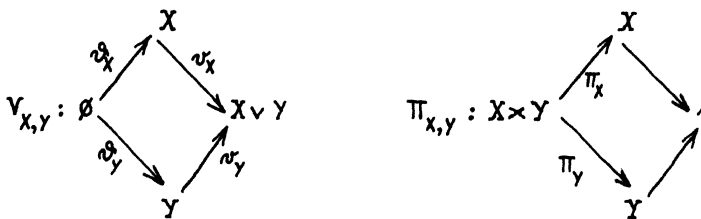
Lemma. Let



be a pull-back-diagram. Then it is a double-diagram iff  $\alpha(X) \cup \beta(Y) = Z$  and  $\alpha/X - \gamma(T)$ ,  $\beta/Y - \sigma(T)$  are injections.

Proof is easy.

XI.4. Lemma. For arbitrary sets  $X, Y$  the diagrams



are double-diagrams.

Proof: Well-known and evident.

XI.5. Theorem. The following properties of a functor  $H$

are equivalent:

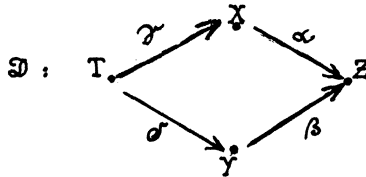
- (i)  $H$  preserves double-diagrams;
- (ii) every component of  $H$  is either naturally equivalent to  $C_1$  or preserves finite sums and finite products.

Proof. We may suppose  $H$  connected.

(i)  $\implies$  (ii): Since  $H$  preserves double-diagrams  $\Pi_{X,Y}$ , it preserves finite products. Consequently either  $H \simeq C_1$  or  $H$  is separating (see IV.4 of [1], note that  $C_{0,1}$  does not preserve double-diagrams).

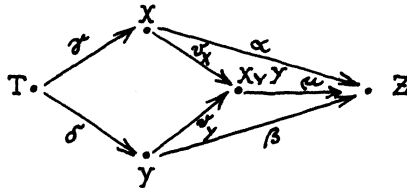
If a separating functor preserves double-diagrams  $V_{X,Y}$ , then it preserves finite sums.

(ii)  $\implies$  (i): Let  $H$  preserve finite sums and finite products. Then  $H$  is separating, consequently it preserves pull-back-diagrams (see VII.10). Let



be a double-diagram.

1) First, we prove that  $[H(\alpha)](H(X)) \cup [H(\beta)](H(Y)) = H(Z)$ . Consider the commutative diagram

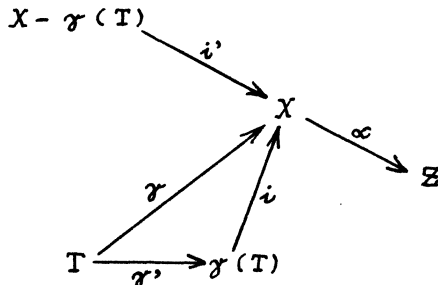


(thus,  $\mu = \text{coeq}(\nu_x \circ \sigma, \nu_y \circ \delta)$ ).  $H(\mu)$

is a surjection since  $\alpha$  is. Now, use  $H(X \vee Y) = H(X) \vee H(Y)$ .

2) Now we prove that  $H(\alpha) / H(X) - [H(\gamma)](H(T))$

is an injection. Consider the following commutative diagram:



where  $i, i'$  are the inclusions,  $\gamma'$  is a surjection. Since  $\alpha \circ i'$  is an injection,  $H(\alpha \circ i')$  is also an injection. Since  $H(X) = H(\gamma(T)) \vee H(X - \gamma(T))$  and  $H(\gamma(T))_X = [H(\gamma)](H(T))$ , we have  $H(X - \gamma(T))_X = H(X) - [H(\gamma)](H(T))$ . Now, use XI.3.

#### R e f e r e n c e s

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