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TABLES FOR THE TWO-SAMPLE MEDIAN TEST

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Summary. The paper contains tables for the non-parametric median test for two samples whose sizes m, n satisfy $3 \leqq m \leqq n$, $m + n \leqq 41$. We tabulate the probabilities of the upper tail of the distribution up to the point where 10% is exceeded for the first time.

Description of the test. Let us have two random samples $X_1, \ldots, X_m$ and $Y_1, \ldots, Y_n$ with densities f_1 and f_2, respectively, and suppose that the notation is chosen so that $m \leqq n$. Our aim is to test the hypothesis H_0 that f_1 and f_2 are identical but otherwise arbitrary against the alternatives of shift in location expressed by $f_1(x) = f(x - \Delta)$, $f_2(x) = f(x)$, where $\Delta > 0$, or $\Delta < 0$ (one-sided alternatives), or $\Delta \neq 0$ (two-sided alternative).

The median test is performed very easily. First, we pool both samples and find the median of this pooled sample. (Since we assume the existence of densities, with probability 1 all the sample values are distinct and the median is defined uniquely.) More formally, if we put $X_{m+1} = Y_1, \ldots, X_{m+n} = Y_n$, and if $X^{(1)} < X^{(2)} < \ldots < X^{(m+n)}$ are the values of the pooled sample $X_1, \ldots, X_m, X_{m+1}, \ldots, X_{m+n}$ arranged in the order of their magnitude, then the median is $X^{((m+n+1)/2)}$ for $m + n$ odd, and $\frac{1}{2}[X^{((m+n)/2)} + X^{((m+n)/2+1)}]$ for $m + n$ even. The test statistic S of our median test is then equal to the number of the values X_i, $i = 1, \ldots, m$, exceeding this median, increased in addition by 0·5 if and only if $m + n$ is odd and the median coincides with some value X_i, $i = 1, \ldots, m$.

In a concise mathematical formula, we can write $S = \sum_{i=1}^{m} a_{m+n}(R_i)$, where R_i is the rank of X_i in the pooled sample $X_1, \ldots, X_m, X_{m+1}, \ldots, X_{m+n}$, and the scores a_{m+n} are given by $a_{m+n}(j) = \frac{1}{2}[\operatorname{sign}(j - \frac{1}{2}(m + n + 1)) + 1]$ for $j = 1, \ldots, m + n$.

We may note that the median test is asymptotically optimum (in the class of all tests) for the above-mentioned two-sample problem of shift in location, if f is of the double-exponential type, i.e. if $f(x) = (2\sigma)^{-1} e^{-|x-\mu|/\sigma}$ (cf. Hájek-Šidák [1], Section III.1.1).

Description of the table. Table 1 should be read one double-column after the other, and we tabulate here the upper tails of the distribution of the statistic S, under H_0, for all pairs m, n such that $3 \leqq m \leqq n$, $m + n \leqq 41$. In each double-column, following the heading m, n, the left column shows possible critical values c_α of S, while the right column shows the corresponding one-sided significance levels $\alpha = 100P\{S \geqq c_\alpha\}$ (i.e. in per cents) rounded off to three decimal places. The tabulation begins by the largest c_α for which the corresponding α (rounded off to three decimal places) is $>0{\cdot}000$, and continues with all possible consecutive values c_α of S until such c_α is reached for which the corresponding α exceeds for the first time 10.000%.

For the computation of Table 1 we used the formula

$$P\{S = k\} = \binom{[\frac{1}{2}(m+n)]}{[k]}\binom{[\frac{1}{2}(m+n)]}{[m-k]}\binom{m+n}{m}^{-1}$$

(where $[x]$ denotes the largest integer not exceeding x), valid for $k = 0, 1, \ldots, m$ whenever $m + n$ is even) and for $k = 0, \frac{1}{2}, \ldots, m - \frac{1}{2}, m$ whenever $m + n$ is odd. (Cf. Hájek-Šidák [1], Theorem IV. 2.1.a.) The present author is deeply indebted to M. Nosál for programming the computation.

It may be observed further, that the distribution (under H_0) of S is symmetric about its mean value $\mathsf{E}S = \frac{1}{2}m$, and its variance is

$$\operatorname{var} S = mn/[4(m + n - 1)] \quad \text{for} \quad m + n \quad \text{even},$$
$$= mn/[4(m + n)] \quad \text{for} \quad m + n \quad \text{odd}.$$

If we are testing H_0 against the one-sided alternative $\Delta > 0$ (i.e. f_1 is shifted to the right with respect to f_2), we use the critical region $\{S \geqq c_\alpha\}$ and the corresponding significance level is the tabulated α. If we are testing against $\Delta < 0$ (i.e. f_1 is shifted to the left), we use the critical region $\{S \leqq m - c_\alpha\}$ whose significance level is again α. If we are testing against the two-sided alternative $\Delta \neq 0$, we use the critical region $\{S \geqq c_\alpha \text{ or } S \leqq m - c_\alpha\}$ whose significance level is equal to 2α.

Example. Let one sample contain the values 81; 105; 33; 78; 126; 61; 88, the other sample the values 32; 83; 50; 59; 10; 45. For the application of our table we must have $m \leqq n$, therefore the latter sample must be denoted as $X_1, \ldots, X_6$, and the former sample as $Y_1, \ldots, Y_7$. The median of the pooled sample is 61. The number of the values X_i exceeding 61 is 1; $m + n$ is odd but the median is one of the values Y_j, so that we shall not add the number 0·5. Therefore $S = 1$. In Table 1 we find for $m = 6$, $n = 7$, $c_\alpha = 5{\cdot}0$ the one-sided significance level $\alpha = 2{\cdot}506\%$. If we are testing against the one-sided alternative $\Delta < 0$, we use the critical region $\{S \leqq 6 - 5\} = \{S \leqq 1\}$ so that H_0 may be rejected at the level $\alpha = 2{\cdot}506\%$. If we are testing against the two-sided alternative $\Delta \neq 0$, we use the critical region $\{S \geqq 5 \text{ or } S \leqq 1\}$ so that H_0 may be rejected at the level $2\alpha = 5{\cdot}012\%$.

Remark on asymptotic normality. For large sizes m, n we may use the normal approximation, since the standardized test statistic $(S - \mathsf{E}S)/(\mathsf{var}\ S)^{1/2}$ has (under H_0) asymptotically the standardized normal distribution whenever $m \to \infty$, $n \to \infty$ in an arbitrary manner (cf. Hájek-Šidák [1], Section III.1.1).

Remark on ties. In practice, equal observations sometimes occur in the samples. In this case, we may use e.g. the following "method of average scores" (cf. Hájek-Šidák [1], Section III.8.1). First, in each group of equal observations, the observations are arranged in some auxiliary ordering, and the median is then found as usually. The only trouble in calculating the value of S arises with the group of observations that are equal to the median; this group will be called the median group, and let it contain a values X_i, and b values Y_j. Further, in our auxiliary ordering, let the median group contain r values preceding the median, and s values exceeding the median.

If $m + n$ is even, the median group has $a + b = r + s$ values, and the average score in it is $(r \cdot 0 + s \cdot 1)/(r + s)$; hence S equals the number of X_i's larger than the median, plus $as/(r + s)$.

If $m + n$ is odd, the median group has $a + b = r + s + 1$ values, and the average score in it is $(r \cdot 0 + \frac{1}{2} + s \cdot 1)/(r + s + 1)$; hence S equals the number of X_i's larger than the median, plus $a(s + \frac{1}{2})/(r + s + 1)$.

If the median group does not contain too many observations, we can still use our Table 1 as an approximation.

Remark on related tests. Several closely related tests have been introduced in the past under the name "median test". E.g. many authors define the "median test" statistic S_0 simply as the number of X_i's larger than the median of the pooled sample (without possible adding $\frac{1}{2}$); however, the distribution of S_0 for $m + n$ odd is not symmetric. In the book [1] and in the present tables we have preferred the statistic S defined above, because the calculation of S is practically not more difficult than that of S_0 but S has two advantages: its distribution is always symmetric, and it offers, for $m + n$ odd, a richer choice of possible significance levels.

Still some other forms of the "median test" statistic have been employed, e.g. those arising from the expression of the problem as a 2×2 contingency table, or the statistic being equal to the number of X_i's exceeding the median of Y_j's (cf. Hájek-Šidák [1], Section III.1.1).

Reference

[1] *J. Hájek, Z. Šidák:* Theory of rank tests. Academia, Prague & Academic Press, New York — London 1967.

Table 1. Critical values c_α of the median test statistic S and significance levels $100\,P\,\{S \geqq c_\alpha\}$ (i.e. in per cents)

$m = 3,\ n = 3$	
3·0	5·000
2·0	50·000
$m = 3,\ n = 4$	
3·0	2·857
2·5	11·429
$m = 3,\ n = 5$	
3·0	7·143
2·0	50·000
$m = 3,\ n = 6$	
3·0	4·762
2·5	11·905
$m = 3,\ n = 7$	
3·0	8·333
2·0	50·000
$m = 3,\ n = 8$	
3·0	6·061
2·5	12·121
$m = 3,\ n = 9$	
3·0	9·091
2·0	50·000
$m = 3,\ n = 10$	
3·0	6·993
2·5	12·238
$m = 3,\ n = 11$	
3·0	9·615
2·0	50·000
$m = 3,\ n = 12$	
3·0	7·692
2·5	12·308
$m = 3,\ n = 13$	
3·0	10·000
2·0	50·000
$m = 3,\ n = 14$	
3·0	8·235
2·5	12·353
$m = 3,\ n = 15$	
3·0	10·294
$m = 3,\ n = 16$	
3·0	8·669
2·5	12·384
$m = 3,\ n = 17$	
3·0	10·526
$m = 3,\ n = 18$	
3·0	9·023
2·5	12·406
$m = 3,\ n = 19$	
3·0	10·714
$m = 3,\ n = 20$	
3·0	9·317
2·5	12·422
$m = 3,\ n = 21$	
3·0	10·870
$m = 3,\ n = 22$	
3·0	9·565
2·5	12·435
$m = 3,\ n = 23$	
3·0	11·000
$m = 3,\ n = 24$	
3·0	9·778
2·5	12·444
$m = 3,\ n = 25$	
3·0	11·111
$m = 3,\ n = 26$	
3·0	9·962
2·5	12·452
$m = 3,\ n = 27$	
3·0	11·207
$m = 3,\ n = 28$	
3·0	10·122
$m = 3,\ n = 29$	
3·0	11·290
$m = 3,\ n = 30$	
3·0	10·264
$m = 3,\ n = 31$	
3·0	11·364
$m = 3,\ n = 32$	
3·0	10·390
$m = 3,\ n = 33$	
3·0	11·429
$m = 3,\ n = 34$	
3·0	10·502
$m = 3,\ n = 35$	
3·0	11·486
$m = 3,\ n = 36$	
3·0	10·603
$m = 3,\ n = 37$	
3·0	11·538
$m = 3,\ n = 38$	
3·0	10·694
$m = 4,\ n = 4$	
4·0	1·429
3·0	24·286
$m = 4,\ n = 5$	
4·0	0·794
3·5	3·968
3·0	16·667
$m = 4,\ n = 6$	
4·0	2·381
3·0	26·190
$m = 4,\ n = 7$	
4·0	1·515
3·5	4·545
3·0	19·697
$m = 4,\ n = 8$	
4·0	3·030
3·0	27·273
$m = 4,\ n = 9$	
4·0	2·098
3·5	4·895
3·0	21·678
$m = 4,\ n = 10$	
4·0	3·497
3·0	27·972
$m = 4,\ n = 11$	
4·0	2·564
3·5	5·128
3·0	23·077
$m = 4,\ n = 12$	
4·0	3·846
3·0	28·462
$m = 4,\ n = 13$	
4·0	2·941
3·5	5·294
3·0	24·118
$m = 4,\ n = 14$	
4·0	4·118
3·0	28·824
$m = 4,\ n = 15$	
4·0	3·251
3·5	5·418
3·0	24·923
$m = 4,\ n = 16$	
4·0	4·334
3·0	29·102
$m = 4,\ n = 17$	
4·0	3·509
3·5	5·514
3·0	25·564
$m = 4,\ n = 18$	
4·0	4·511
3·0	29·323
$m = 4,\ n = 19$	
4·0	3·727
3·5	5·590
3·0	26·087
$m = 4,\ n = 20$	
4·0	4·658
3·0	29·503
$m = 4,\ n = 21$	
4·0	3·913
3·5	5·652
3·0	26·522

$m = 4,\ n = 22$	
4·0	4·783
3·0	29·652
$m = 4,\ n = 23$	
4·0	4·074
3·5	5·704
3·0	26·889
$m = 4,\ n = 24$	
4·0	4·889
3·0	29·778
$m = 4,\ n = 25$	
4·0	4·215
3·5	5·747
3·0	27·203
$m = 4,\ n = 26$	
4·0	4·981
3·0	29·885
$m = 4,\ n = 27$	
4·0	4·338
3·5	5·784
3·0	27·475
$m = 4,\ n = 28$	
4·0	5·061
3·0	29·978
$m = 4,\ n = 29$	
4·0	4·448
3·5	5·816
3·0	27·713
$m = 4,\ n = 30$	
4·0	5·132
3·0	30·059
$m = 4,\ n = 31$	
4·0	4·545
3·5	5·844
3·0	27·922
$m = 4,\ n = 32$	
4·0	5·195
3·0	30·130
$m = 4,\ n = 33$	
4·0	4·633
3·5	5·869
3·0	28·108

$m = 4,\ n = 34$	
4·0	5·251
3·0	30·193
$m = 4,\ n = 35$	
4·0	4·712
3·5	5·891
3·0	28·274
$m = 4,\ n = 36$	
4·0	5·301
3·0	30·249
$m = 4,\ n = 37$	
4·0	4·784
3·5	5·910
3·0	28·424
$m = 5,\ n = 5$	
5·0	0·397
4·0	10·317
$m = 5,\ n = 6$	
5·0	0·216
4·5	1·299
4·0	6·710
3·5	17·532
$m = 5,\ n = 7$	
5·0	0·758
4·0	12·121
$m = 5,\ n = 8$	
5·0	0·466
4·5	1·632
4·0	8·625
3·5	17·949
$m = 5,\ n = 9$	
5·0	1·049
4·0	13·287
$m = 5,\ n = 10$	
5·0	0·699
4·5	1·865
4·0	10·023
$m = 5,\ n = 11$	
5·0	1·282
4·0	14·103

$m = 5,\ n = 12$	
5·0	0·905
4·5	2·036
4·0	11·086
$m = 5,\ n = 13$	
5·0	1·471
4·0	14·706
$m = 5,\ n = 14$	
5·0	1·084
4·5	2·167
4·0	11·920
$m = 5,\ n = 15$	
5·0	1·625
4·0	15·170
$m = 5,\ n = 16$	
5·0	1·238
4·5	2·270
4·0	12·590
$m = 5,\ n = 17$	
5·0	1·754
4·0	15·539
$m = 5,\ n = 18$	
5·0	1·373
4·5	2·354
4·0	13·142
$m = 5,\ n = 19$	
5·0	1·863
4·0	15·839
$m = 5,\ n = 20$	
5·0	1·491
4·5	2·422
4·0	13·602
$m = 5,\ n = 21$	
5·0	1·957
4·0	16·087
$m = 5,\ n = 22$	
5·0	1·594
4·5	2·480
4·0	13·994
$m = 5,\ n = 23$	
5·0	2·037
4·0	16·296

$m = 5,\ n = 24$	
5·0	1·686
4·5	2·529
4·0	14·330
$m = 5,\ n = 25$	
5·0	2·107
4·0	16·475
$m = 5,\ n = 26$	
5·0	1·767
4·5	2·571
4·0	14·621
$m = 5,\ n = 27$	
5·0	2·169
4·0	16·630
$m = 5,\ n = 28$	
5·0	1·840
4·5	2·607
4·0	14·877
$m = 5,\ n = 29$	
5·0	2·224
4·0	16·764
$m = 5,\ n = 30$	
5·0	1·906
4·5	2·639
4·0	15·103
$m = 5,\ n = 31$	
5·0	2·273
4·0	16·883
$m = 5,\ n = 32$	
5·0	1·966
4·5	2·668
4·0	15·304
$m = 5,\ n = 33$	
5·0	2·317
4·0	16·988
$m = 5,\ n = 34$	
5·0	2·020
4·5	2·693
4·0	15·484
$m = 5,\ n = 35$	
5·0	2·356
4·0	17·082

$m = 5$, $n = 36$	
5·0	2·069
4·5	2·715
4·0	15·646

$m = 6$, $n = 6$	
6·0	0·108
5·0	4·004
4·0	28·355

$m = 6$, $n = 7$	
6·0	0·058
5·5	0·408
5·0	2·506
4·5	7·751
4·0	20·862

$m = 6$, $n = 8$	
6·0	0·233
5·0	5·128
4·0	29·604

$m = 6$, $n = 9$	
6·0	0·140
5·5	0·559
5·0	3·497
4·5	8·392
4·0	23·077

$m = 6$, $n = 10$	
6·0	0·350
5·0	5·944
4·0	30·420

$m = 6$, $n = 11$	
6·0	0·226
5·5	0·679
5·0	4·299
4·5	8·824
4·0	24·661

$m = 6$, $n = 12$	
6·0	0·452
5·0	6·561
4·0	30·995

$m = 6$, $n = 13$	
6·0	0·310
5·5	0·774
5·0	4·954
4·5	9·133
4·0	25·851

$m = 6$, $n = 14$	
6·0	0·542
5·0	7·043
4·0	31·424

$m = 6$, $n = 15$	
6·0	0·387
5·5	0·851
5·0	5·495
4·5	9·365
4·0	26·780

$m = 6$, $n = 16$	
6·0	0·619
5·0	7·430
4·0	31·756

$m = 6$, $n = 17$	
6·0	0·458
5·5	0·915
5·0	5·950
4·5	9·546
4·0	27·525

$m = 6$, $n = 18$	
6·0	0·686
5·0	7·748
4·0	32·020

$m = 6$, $n = 19$	
6·0	0·522
5·5	0·969
5·0	6·335
4·5	9·689
4·0	28·137

$m = 6$, $n = 20$	
6·0	0·745
5·0	8·012
4·0	32·236

$m = 6$, $n = 21$	
6·0	0·580
5·5	1·014
5·0	6·667
4·5	9·807
4·0	28·647

$m = 6$, $n = 22$	
6·0	0·797
5·0	8·237
4·0	32·415

$m = 6$, $n = 23$	
6·0	0·632
5·5	1·054
5·0	6·954
4·5	9·904
4·0	29·080

$m = 6$, $n = 24$	
6·0	0·843
5·0	8·429
4·0	32·567

$m = 6$, $n = 25$	
6·0	0·680
5·5	1·088
5·0	7·206
4·5	9·986
4·0	29·452

$m = 6$, $n = 26$	
6·0	0·884
5·0	8·596
4·0	32·697

$m = 6$, $n = 27$	
6·0	0·723
5·5	1·117
5·0	7·427
4·5	10·057

$m = 6$, $n = 28$	
6·0	0·920
5·0	8·742
4·0	32·809

$m = 6$, $n = 29$	
6·0	0·762
5·5	1·144
5·0	7·625
4·5	10·117

$m = 6$, $n = 30$	
6·0	0·953
5·0	8·871
4·0	32·907

$m = 6$, $n = 31$	
6·0	0·799
5·5	1·167
5·0	7·801
4·5	10·170

$m = 6$, $n = 32$	
6·0	0·983
5·0	8·986
4·0	32·994

$m = 6$, $n = 33$	
6·0	0·832
5·5	1·188
5·0	7·960
4·5	10·217

$m = 6$, $n = 34$	
6·0	1·010
5·0	9·088
4·0	33·071

$m = 6$, $n = 35$	
6·0	0·862
5·5	1·207
5·0	8·103
4·5	10·258

$m = 7$, $n = 7$	
7·0	0·029
6·0	1·457
5·0	14·307

$m = 7$, $n = 8$	
7·0	0·016
6·5	0·124
6·0	0·886
5·5	3·170
5·0	10·023

$m = 7$, $n = 9$	
7·0	0·070
6·0	2·028
5·0	15·734

$m = 7$, $n = 10$	
7·0	0·041
6·5	0·185
6·0	1·337
5·5	3·640
5·0	11·703

$m = 7$, $n = 11$	
7·0	0·113
6·0	2·489
5·0	16·742

$m = 7,\ n = 12$	
7·0	0·071
6·5	0·238
6·0	1·739
5·5	3·989
5·0	12·991

$m = 7,\ n = 13$	
7·0	0·155
6·0	2·864
5·0	17·492

$m = 7,\ n = 14$	
7·0	0·103
6·5	0·284
6·0	2·090
5·5	4·257
5·0	14·009

$m = 7,\ n = 15$	
7·0	0·193
6·0	3·173
5·0	18·073

$m = 7,\ n = 16$	
7·0	0·135
6·5	0·323
6·0	2·396
5·5	4·469
5·0	14·834

$m = 7,\ n = 17$	
7·0	0·229
6·0	3·432
5·0	18·535

$m = 7,\ n = 18$	
7·0	0·165
6·5	0·357
6·0	2·664
5·5	4·641
5·0	15·515

$m = 7,\ n = 19$	
7·0	0·261
6·0	3·652
5·0	18·913

$m = 7,\ n = 20$	
7·0	0·193
6·5	0·386
6·0	2·899
5·5	4·783
5·0	16·087

$m = 7,\ n = 21$	
7·0	0·290
6·0	3·841
5·0	19·227

$m = 7,\ n = 22$	
7·0	0·220
6·5	0·412
6·0	3·106
5·5	4·902
5·0	16·574

$m = 7,\ n = 23$	
7·0	0·316
6·0	4·004
5·0	19·492

$m = 7,\ n = 24$	
7·0	0·245
6·5	0·435
6·0	3·290
5·5	5·003
5·0	16·994

$m = 7,\ n = 25$	
7·0	0·340
6·0	4·147
5·0	19·719

$m = 7,\ n = 26$	
7·0	0·268
6·5	0·455
6·0	3·454
5·5	5·090
5·0	17·360

$m = 7,\ n = 27$	
7·0	0·362
6·0	4·272
5·0	19·916

$m = 7,\ n = 28$	
7·0	0·289
6·5	0·473
6·0	3·602
5·5	5·166
5·0	17·681

$m = 7,\ n = 29$	
7·0	0·381
6·0	4·384
5·0	20·088

$m = 7,\ n = 30$	
7·0	0·309
6·5	0·489
6·0	3·735
5·5	5·233
5·0	17·966

$m = 7,\ n = 31$	
7·0	0·399
6·0	4·484
5·0	20·240

$m = 7,\ n = 32$	
7·0	0·328
6·5	0·504
6·0	3·856
5·5	5·292
5·0	18·220

$m = 7,\ n = 33$	
7·0	0·416
6·0	4·574
5·0	20·374

$m = 7,\ n = 34$	
7·0	0·345
6·5	0·517
6·0	3·965
5·5	5·345
5·0	18·447

$m = 8,\ n = 8$	
8·0	0·008
7·0	0·505
6·0	6·597
5·0	30·963

$m = 8,\ n = 9$	
8·0	0·004
7·5	0·037
7·0	0·300
6·5	1·222
6·0	4·447
5·5	10·897

$m = 8,\ n = 10$	
8·0	0·021
7·0	0·761
6·0	7·672
5·0	31·859

$m = 8,\ n = 11$	
8·0	0·012
7·5	0·060
7·0	0·488
6·5	1·488
6·0	5·489
5·5	11·491

$m = 8,\ n = 12$	
8·0	0·036
7·0	0·988
6·0	8·490
5·0	32·496

$m = 8,\ n = 13$	
8·0	0·022
7·5	0·081
7·0	0·671
6·5	1·703
6·0	6·347
5·5	11·920

$m = 8,\ n = 14$	
8·0	0·052
7·0	1·187
6·0	9·133
5·0	32·972

$m = 8,\ n = 15$	
8·0	0·034
7·5	0·101
7·0	0·841
6·5	1·878
6·0	7·060
5·5	12·243

$m = 8,\ n = 16$	
8·0	0·067
7·0	1·360
6·0	9·651
5·0	33·342

$m = 8,\ n = 17$	
8·0	0·046
7·5	0·119
7·0	0·998
6·5	2·023
6·0	7·661
5·5	12·494

$m = 8,\ n = 18$	
8·0	0·082
7·0	1·510
6·0	10·078

$m = 8,\ n = 19$	
8·0	0·058
7·5	0·135
7·0	1·140
6·5	2·145
6·0	8·174
5·5	12·696

$m = 8,\ n = 20$	
8·0	0·097
7·0	1·643
6·0	10·435

$m = 8,\ n = 21$	
8·0	0·070
7·5	0·150
7·0	1·269
6·5	2·249
6·0	8·616
5·5	12·860

$m = 8,\ n = 22$	
8·0	0·110
7·0	1·759
6·0	10·738

$m = 8,\ n = 23$	
8·0	0·082
7·5	0·163
7·0	1·387
6·5	2·338
6·0	9·000
5·5	12·997

$m = 8,\ n = 24$	
8·0	0·122
7·0	1·863
6·0	10·999

$m = 8,\ n = 25$	
8·0	0·093
7·5	0·175
7·0	1·493
6·5	2·416
6·0	9·338
5·5	13·113

$m = 8,\ n = 26$	
8·0	0·134
7·0	1·955
6·0	11·225

$m = 8,\ n = 27$	
8·0	0·103
7·5	0·186
7·0	1·591
6·5	2·485
6·0	9·636
5·5	13·212

$m = 8,\ n = 28$	
8·0	0·145
7·0	2·038
6·0	11·424

$m = 8,\ n = 29$	
8·0	0·113
7·5	0·196
7·0	1·679
6·5	2·545
6·0	9·902
5·5	13·297

$m = 8,\ n = 30$	
8·0	0·155
7·0	2·112
6·0	11·599

$m = 8,\ n = 31$	
8·0	0·123
7·5	0·205
7·0	1·761
6·5	2·599
6·0	10·140

$m = 8,\ n = 32$	
8·0	0·164
7·0	2·180
6·0	11·756

$m = 8,\ n = 33$	
8·0	0·132
7·5	0·213
7·0	1·836
6·5	2·647
6·0	10·354

$m = 9,\ n = 9$	
9·0	0·002
8·0	0·169
7·0	2·834
6·0	17·347

$m = 9,\ n = 10$	
9·0	0·001
8·5	0·011
8·0	0·099
7·5	0·449
7·0	1·852
6·5	5·126
6·0	12·764

$m = 9,\ n = 11$	
9·0	0·006
8·0	0·274
7·0	3·489
6·0	18·492

$m = 9,\ n = 12$	
9·0	0·003
8·5	0·019
8·0	0·172
7·5	0·580
7·0	2·417
6·5	5·632
6·0	14·206

$m = 9,\ n = 13$	
9·0	0·011
8·0	0·376
7·0	4·025
6·0	19·350

$m = 9,\ n = 14$	
9·0	0·007
8·5	0·027
8·0	0·249
7·5	0·693
7·0	2·914
6·5	6·024
6·0	15·352

$m = 9,\ n = 15$	
9·0	0·017
8·0	0·471
7·0	4·469
6·0	20·016

$m = 9,\ n = 16$	
9·0	0·011
8·5	0·035
8·0	0·326
7·5	0·791
7·0	3·350
6·5	6·335
6·0	16·285

$m = 9,\ n = 17$	
9·0	0·023
8·0	0·558
7·0	4·842
6·0	20·549

$m = 9,\ n = 18$	
9·0	0·015
8·5	0·043
8·0	0·400
7·5	0·876
7·0	3·732
6·5	6·587
6·0	17·059

$m = 9,\ n = 19$	
9·0	0·029
8·0	0·638
7·0	5·159
6·0	20·986

$m = 9,\ n = 20$	
9·0	0·020
8·5	0·050
8·0	0·470
7·5	0·950
7·0	4·068
6·5	6·797
6·0	17·711

$m = 9,\ n = 21$	
9·0	0·035
8·0	0·710
7·0	5·432
6·0	21·349

$m = 9,\ n = 22$	
9·0	0·025
8·5	0·057
8·0	0·536
7·5	1·014
7·0	4·366
6·5	6·973
6·0	18·269

$m = 9$, $n = 23$	
9·0	0·041
8·0	0·775
7·0	5·669
6·0	21·657

$m = 9$, $n = 24$	
9·0	0·030
8·5	0·063
8·0	0·597
7·5	1·072
7·0	4·631
6·5	7·123
6·0	18·750

$m = 9$, $n = 25$	
9·0	0·046
8·0	0·834
7·0	5·877
6·0	21·922

$m = 9$, $n = 26$	
9·0	0·034
8·5	0·069
8·0	0·654
7·5	1·122
7·0	4·868
6·5	7·252
6·0	19·171

$m = 9$, $n = 27$	
9·0	0·052
8·0	0·888
7·0	6·060
6·0	22·151

$m = 9$, $n = 28$	
9·0	0·039
8·5	0·074
8·0	0·707
7·5	1·168
7·0	5·082
6·5	7·365
6·0	19·542

$m = 9$, $n = 29$	
9·0	0·057
8·0	0·938
7·0	6·223
6·0	22·352

$m = 9$, $n = 30$	
9·0	0·044
8·5	0·079
8·0	0·757
7·5	1·209
7·0	5·275
6·5	7·464
6·0	19·870

$m = 9$, $n = 31$	
9·0	0·061
8·0	0·983
7·0	6·369
6·0	22·529

$m = 9$, $n = 32$	
9·0	0·048
8·5	0·084
8·0	0·803
7·5	1·246
7·0	5·450
6·5	7·552
6·0	20·164

$m = 10$, $n = 10$	
10·0	0·001
9·0	0·055
8·0	1·151
7·0	8·945
6·0	32·814

$m = 10$, $n = 11$	
9·5	0·003
9·0	0·031
8·5	0·159
8·0	0·733
7·5	2·264
7·0	6·347
6·5	13·491

$m = 10$, $n = 12$	
10·0	0·002
9·0	0·095
8·0	1·499
7·0	9·919
6·0	33·496

$m = 10$, $n = 13$	
10·0	0·001
9·5	0·006
9·0	0·059
8·5	0·217
8·0	1·011
7·5	2·597
7·0	7·356
6·5	14·019

$m = 10$, $n = 14$	
10·0	0·003
9·0	0·138
8·0	1·804
7·0	10·688

$m = 10$, $n = 15$	
10·0	0·002
9·5	0·009
9·0	0·090
8·5	0·271
8·0	1·271
7·5	2·870
7·0	8·200
6·5	14·419

$m = 10$, $n = 16$	
10·0	0·005
9·0	0·180
8·0	2·070
7·0	11·310

$m = 10$, $n = 17$	
10·0	0·003
9·5	0·012
9·0	0·122
8·5	0·320
8·0	1·510
7·5	3·097
7·0	8·914
6·5	14·732

$m = 10$, $n = 18$	
10·0	0·008
9·0	0·221
8·0	2·304
7·0	11·823

$m = 10$, $n = 19$	
10·0	0·005
9·5	0·015
9·0	0·155
8·5	0·365
8·0	1·729
7·5	3·288
7·0	9·525
6·5	14·983

$m = 10$, $n = 20$	
10·0	0·010
9·0	0·260
8·0	2·509
7·0	12·254

$m = 10$, $n = 21$	
10·0	0·007
9·5	0·018
9·0	0·187
8·5	0·405
8·0	1·928
7·5	3·452
7·0	10·053

$m = 10$, $n = 22$	
10·0	0·012
9·0	0·296
8·0	2·690
7·0	12·621

$m = 10$, $n = 23$	
10·0	0·009
9·5	0·021
9·0	0·219
8·5	0·441
8·0	2·110
7·5	3·593
7·0	10·514

$m = 10$, $n = 24$	
10·0	0·015
9·0	0·330
8·0	2·851
7·0	12·937

$m = 10$, $n = 25$	
10·0	0·011
9·5	0·024
9·0	0·249
8·5	0·474
8·0	2·275
7·5	3·716
7·0	10·920

$m = 10$, $n = 26$	
10·0	0·017
9·0	0·362
8·0	2·995
7·0	13·212

$m = 10$, $n = 27$	
10·0	0·013
9·5	0·027
9·0	0·278
8·5	0·504
8·0	2·426
7·5	3·824
7·0	11·279
$m = 10$, $n = 28$	
10·0	0·020
9·0	0·391
8·0	3·125
7·0	13·453
$m = 10$, $n = 29$	
10·0	0·015
9·5	0·029
9·0	0·305
8·5	0·531
8·0	2·564
7·5	3·919
7·0	11·599
$m = 10$, $n = 30$	
10·0	0·022
9·0	0·418
8·0	3·242
7·0	13·667
$m = 10$, $n = 31$	
10·0	0·016
9·5	0·031
9·0	0·331
8·5	0·556
8·0	2·691
7·5	4·004
7·0	11·887
$m = 11$, $n = 11$	
10·0	0·017
9·0	0·446
8·0	4·305
7·0	19·743
$m = 11$, $n = 12$	
10·5	0·001
10·0	0·010
9·5	0·055
9·0	0·278
8·5	0·950
8·0	2·963
7·5	6·990
7·0	15·044
$m = 11$, $n = 13$	
10·0	0·032
9·0	0·614
8·0	4·977
7·0	20·682
$m = 11$, $n = 14$	
10·5	0·002
10·0	0·020
9·5	0·079
9·0	0·404
8·5	1·137
8·0	3·581
7·5	7·490
7·0	16·285
$m = 11$, $n = 15$	
11·0	0·001
10·0	0·049
9·0	0·771
8·0	5·535
7·0	21·415
$m = 11$, $n = 16$	
11·0	0·001
10·5	0·003
10·0	0·031
9·5	0·103
9·0	0·530
8·5	1·300
8·0	4·123
7·5	7·888
7·0	17·298
$m = 11$, $n = 17$	
11·0	0·002
10·0	0·067
9·0	0·915
8·0	6·006
7·0	22·004
$m = 11$, $n = 18$	
11·0	0·001
10·5	0·004
10·0	0·044
9·5	0·125
9·0	0·652
8·5	1·442
8·0	4·601
7·5	8·212
7·0	18·142
$m = 11$, $n = 19$	
11·0	0·002
10·0	0·085
9·0	1·047
8·0	6·407
7·0	22·486
$m = 11$, $n = 20$	
11·0	0·002
10·5	0·005
10·0	0·058
9·5	0·147
9·0	0·768
8·5	1·566
8·0	5·024
7·5	8·482
7·0	18·855
$m = 11$, $n = 21$	
11·0	0·003
10·0	0·103
9·0	1·167
8·0	6·753
7·0	22·890
$m = 11$, $n = 22$	
11·0	0·002
10·5	0·006
10·0	0·073
9·5	0·167
9·0	0·876
8·5	1·674
8·0	5·398
7·5	8·709
7·0	19·467
$m = 11$, $n = 23$	
11·0	0·004
10·0	0·120
9·0	1·275
8·0	7·054
7·0	23·232
$m = 11$, $n = 24$	
11·0	0·003
10·5	0·008
10·0	0·087
9·5	0·186
9·0	0·978
8·5	1·771
8·0	5·733
7·5	8·902
7·0	19·996
$m = 11$, $n = 25$	
11·0	0·005
10·0	0·136
9·0	1·375
8·0	7·318
7·0	23·526
$m = 11$, $n = 26$	
11·0	0·004
10·5	0·009
10·0	0·101
9·5	0·203
9·0	1·073
8·5	1·856
8·0	6·033
7·5	9·070
7·0	20·460
$m = 11$, $n = 27$	
11·0	0·006
10·0	0·152
9·0	1·465
8·0	7·551
7·0	23·782
$m = 11$, $n = 28$	
11·0	0·005
10·5	0·010
10·0	0·115
9·5	0·219
9·0	1·162
8·5	1·933
8·0	6·303
7·5	9·216
7·0	20·869
$m = 11$, $n = 29$	
11·0	0·007
10·0	0·167
9·0	1·548
8·0	7·759
7·0	24·006

$m = 11$,	$n = 30$
11·0	0·005
10·5	0·011
10·0	0·128
9·5	0·234
9·0	1·244
8·5	2·002
8·0	6·547
7·5	9·344
7·0	21·232

$m = 12$,	$n = 12$
11·0	0·005
10·0	0·166
9·0	1·956
8·0	11·017

$m = 12$,	$n = 13$
11·0	0·003
10·5	0·018
10·0	0·102
9·5	0·381
9·0	1·312
8·5	3·406
8·0	8·118
7·5	15·657

$m = 12$,	$n = 14$
11·0	0·011
10·0	0·242
9·0	2·359
8·0	11·887

$m = 12$,	$n = 15$
11·5	0·001
11·0	0·006
10·5	0·028
10·0	0·156
9·5	0·477
9·0	1·653
8·5	3·771
8·0	9·064
7·5	16·122

$m = 12$,	$n = 16$
11·0	0·017
10·0	0·316
9·0	2·712
8·0	12·593

$m = 12$,	$n = 17$
11·5	0·001
11·0	0·011
10·5	0·038
10·0	0·213
9·5	0·564
9·0	1·968
8·5	4·075
8·0	9·867
7·5	16·487

$m = 12$,	$n = 18$
12·0	0·001
11·0	0·024
10·0	0·389
9·0	3·022
8·0	13·177

$m = 12$,	$n = 19$
11·5	0·001
11·0	0·016
10·5	0·048
10·0	0·271
9·5	0·644
9·0	2·257
8·5	4·332
8·0	10·556

$m = 12$,	$n = 20$
12·0	0·001
11·0	0·032
10·0	0·457
9·0	3·295
8·0	13·668

$m = 12$,	$n = 21$
12·0	0·001
11·5	0·002
11·0	0·021
10·5	0·058
10·0	0·328
9·5	0·715
9·0	2·521
8·5	4·552
8·0	11·154

$m = 12$,	$n = 22$
12·0	0·001
11·0	0·039
10·0	0·522
9·0	3·536
8·0	14·088

$m = 12$,	$n = 23$
12·0	0·001
11·5	0·002
11·0	0·027
10·5	0·067
10·0	0·384
9·5	0·780
9·0	2·761
8·5	4·742
8·0	11·676

$m = 12$,	$n = 24$
12·0	0·001
11·0	0·047
10·0	0·582
9·0	3·752
8·0	14·449

$m = 12$,	$n = 25$
12·0	0·001
11·5	0·003
11·0	0·034
10·5	0·076
10·0	0·438
9·5	0·839
9·0	2·981
8·5	4·908
8·0	12·136

$m = 12$,	$n = 26$
12·0	0·002
11·0	0·055
10·0	0·638
9·0	3·945
8·0	14·765

$m = 12$,	$n = 27$
12·0	0·001
11·5	0·003
11·0	0·040
10·5	0·085
10·0	0·489
9·5	0·893
9·0	3·182
8·5	5·054
8·0	12·545

$m = 12$,	$n = 28$
12·0	0·002
11·0	0·062
10·0	0·691
9·0	4·118
8·0	15·042

$m = 12$,	$n = 29$
12·0	0·002
11·5	0·004
11·0	0·046
10·5	0·093
10·0	0·537
9·5	0·941
9·0	3·366
8·5	5·184
8·0	12·911

$m = 13$,	$n = 13$
12·0	0·002
11·0	0·060
10·0	0·847
9·0	5·762
8·0	21·688

$m = 13$,	$n = 14$
12·0	0·001
11·5	0·006
11·0	0·036
10·5	0·148
10·0	0·555
9·5	1·575
9·0	4·123
8·5	8·711
8·0	16·969

$m = 13$,	$n = 15$
12·0	0·003
11·0	0·092
10·0	1·065
9·0	6·417
8·0	22·474

$m = 13$,	$n = 16$
12·0	0·002
11·5	0·010
11·0	0·058
10·5	0·193
10·0	0·729
9·5	1·803
9·0	4·756
8·5	9·186
8·0	18·045

$m = 13$,	$n = 17$
12·0	0·006
11·0	0·125
10·0	1·266
9·0	6·971
8·0	23·107

$m = 13,\ n = 18$	
12·0	0·004
11·5	0·014
11·0	0·083
10·5	0·236
10·0	0·898
9·5	2·002
9·0	5·315
8·5	9·574
8·0	18·943

$m = 13,\ n = 19$	
12·0	0·009
11·0	0·159
10·0	1·450
9·0	7·444
8·0	23·627

$m = 13,\ n = 20$	
12·0	0·005
11·5	0·018
11·0	0·109
10·5	0·277
10·0	1·059
9·5	2·177
9·0	5·810
8·5	9·896
8·0	19·704

$m = 13,\ n = 21$	
12·0	0·012
11·0	0·193
10·0	1·618
9·0	7·853
8·0	24·063

$m = 13,\ n = 22$	
12·5	0·001
12·0	0·008
11·5	0·022
11·0	0·136
10·5	0·315
10·0	1·211
9·5	2·331
9·0	6·250
8·5	10·169

$m = 13,\ n = 23$	
12·0	0·015
11·0	0·226
10·0	1·771
9·0	8·209
8·0	24·434

$m = 13,\ n = 24$	
12·5	0·001
12·0	0·010
11·5	0·026
11·0	0·163
10·5	0·351
10·0	1·353
9·5	2·467
9·0	6·643
8·5	10·402

$m = 13,\ n = 25$	
13·0	0·001
12·0	0·018
11·0	0·257
10·0	1·910
9·0	8·522
8·0	24·753

$m = 13,\ n = 26$	
12·5	0·001
12·0	0·013
11·5	0·030
11·0	0·190
10·5	0·384
10·0	1·486
9·5	2·588
9·0	6·996
8·5	10·603

$m = 13,\ n = 27$	
13·0	0·001
12·0	0·022
11·0	0·287
10·0	2·037
9·0	8·800
8·0	25·030

$m = 13,\ n = 28$	
12·5	0·001
12·0	0·015
11·5	0·035
11·0	0·216
10·5	0·415
10·0	1·610
9·5	2·697
9·0	7·315
8·5	10·779

$m = 14,\ n = 14$	
12·0	0·021
11·0	0·351
10·0	2·849
9·0	12·840

$m = 14,\ n = 15$	
12·5	0·002
12·0	0·013
11·5	0·055
11·0	0·226
10·5	0·696
10·0	1·988
9·5	4·572
9·0	9·739
8·5	17·491

$m = 14,\ n = 16$	
13·0	0·001
12·0	0·034
11·0	0·461
10·0	3·280
9·0	13·615

$m = 14,\ n = 17$	
13·0	0·001
12·5	0·003
12·0	0·021
11·5	0·075
11·0	0·309
10·5	0·825
10·0	2·371
9·5	4·947
9·0	10·615

$m = 14,\ n = 18$	
13·0	0·002
12·0	0·048
11·0	0·567
10·0	3·659
9·0	14·258

$m = 14,\ n = 19$	
13·0	0·001
12·5	0·005
12·0	0·031
11·5	0·095
11·0	0·394
10·5	0·942
10·0	2·722
9·5	5·265
9·0	11·367

$m = 14,\ n = 20$	
13·0	0·003
12·0	0·063
11·0	0·668
10·0	3·993
9·0	14·800

$m = 14,\ n = 21$	
13·0	0·002
12·5	0·006
12·0	0·043
11·5	0·115
11·0	0·478
10·5	1·048
10·0	3·043
9·5	5·537
9·0	12·021

$m = 14,\ n = 22$	
13·0	0·004
12·0	0·079
11·0	0·763
10·0	4·290
9·0	15·263

$m = 14,\ n = 23$	
13·0	0·003
12·5	0·008
12·0	0·055
11·5	0·134
11·0	0·560
10·5	1·144
10·0	3·337
9·5	5·773
9·0	12·594

$m = 14,\ n = 24$	
13·0	0·005
12·0	0·095
11·0	0·852
10·0	4·555
9·0	15·664

$m = 14,\ n = 25$	
13·0	0·004
12·5	0·010
12·0	0·067
11·5	0·153
11·0	0·638
10·5	1·232
10·0	3·605
9·5	5·979
9·0	13·100

$m = 14$, $n = 26$	
13·0	0·007
12·0	0·110
11·0	0·935
10·0	4·792
9·0	16·013
$m = 14$, $n = 27$	
13·0	0·005
12·5	0·012
12·0	0·080
11·5	0·170
11·0	0·714
10·5	1·311
10·0	3·851
9·5	6·161
9·0	13·550
$m = 15$, $n = 15$	
13·0	0·007
12·0	0·141
11·0	1·342
10·0	7·156
9·0	23·305
$m = 15$, $n = 16$	
13·5	0·001
13·0	0·004
12·5	0·020
12·0	0·089
11·5	0·296
11·0	0·916
10·5	2·280
10·0	5·280
9·5	10·281
$m = 15$, $n = 17$	
13·0	0·012
12·0	0·192
11·0	1·598
10·0	7·781
9·0	23·974
$m = 15$, $n = 18$	
13·5	0·001
13·0	0·008
12·5	0·029
12·0	0·127
11·5	0·363
11·0	1·129
10·5	2·534
10·0	5·907
9·5	10·725
$m = 15$, $n = 19$	
14·0	0·001
13·0	0·018
12·0	0·245
11·0	1·832
10·0	8·316
9·0	24·526
$m = 15$, $n = 20$	
13·5	0·002
13·0	0·012
12·5	0·038
12·0	0·167
11·5	0·426
11·0	1·333
10·5	2·758
10·0	6·463
9·5	11·095
$m = 15$, $n = 21$	
14·0	0·001
13·0	0·025
12·0	0·297
11·0	2·046
10·0	8·779
9·0	24·990
$m = 15$, $n = 22$	
14·0	0·001
13·5	0·002
13·0	0·016
12·5	0·047
12·0	0·208
11·5	0·486
11·0	1·526
10·5	2·956
10·0	6·959
9·5	11·408
$m = 15$, $n = 23$	
14·0	0·001
13·0	0·031
12·0	0·347
11·0	2·241
10·0	9·184
9·0	25·384
$m = 15$, $n = 24$	
14·0	0·001
13·5	0·003
13·0	0·021
12·5	0·056
12·0	0·250
11·5	0·541
11·0	1·707
10·5	3·131
10·0	7·403
9·5	11·676
$m = 15$, $n = 25$	
14·0	0·002
13·0	0·039
12·0	0·396
11·0	2·419
10·0	9·540
9·0	25·724
$m = 15$, $n = 26$	
14·0	0·001
13·5	0·004
13·0	0·027
12·5	0·065
12·0	0·291
11·5	0·593
11·0	1·876
10·5	3·287
10·0	7·803
9·5	11·908
$m = 16$, $n = 16$	
14·0	0·002
13·0	0·055
12·0	0·606
11·0	3·780
10·0	14·449
$m = 16$, $n = 17$	
14·0	0·001
13·5	0·007
13·0	0·034
12·5	0·121
12·0	0·405
11·5	1·087
11·0	2·722
10·5	5·720
10·0	11·216
$m = 16$, $n = 18$	
14·0	0·004
13·0	0·078
12·0	0·746
11·0	4·221
10·0	15·141
$m = 16$, $n = 19$	
14·0	0·003
13·5	0·011
13·0	0·050
12·5	0·154
12·0	0·517
11·5	1·242
11·0	3·129
10·5	6·093
10·0	12·021
$m = 16$, $n = 20$	
14·0	0·007
13·0	0·102
12·0	0·880
11·0	4·611
10·0	15·726
$m = 16$, $n = 21$	
14·5	0·001
14·0	0·004
13·5	0·014
13·0	0·069
12·5	0·186
12·0	0·627
11·5	1·384
11·0	3·501
10·5	6·413
10·0	12·722
$m = 16$, $n = 22$	
14·0	0·009
13·0	0·127
12·0	1·006
11·0	4·957
10·0	16·227

$m = 16,\ n = 23$

14·5	0·001
14·0	0·006
13·5	0·018
13·0	0·088
12·5	0·218
12·0	0·735
11·5	1·512
11·0	3·843
10·5	6·691
10·0	13·338

$m = 16,\ n = 24$

15·0	0·001
14·0	0·012
13·0	0·153
12·0	1·124
11·0	5·267
10·0	16·661

$m = 16,\ n = 25$

14·5	0·001
14·0	0·008
13·5	0·023
13·0	0·108
12·5	0·248
12·0	0·840
11·5	1·629
11·0	4·155
10·5	6·934
10·0	13·882

$m = 17,\ n = 17$

15·0	0·001
14·0	0·021
13·0	0·263
12·0	1·904
11·0	8·468
10·0	24·675

$m = 17,\ n = 18$

14·5	0·003
14·0	0·013
13·5	0·048
13·0	0·173
12·5	0·498
12·0	1·342
11·5	3·029
11·0	6·405
10·5	11·709

$m = 17,\ n = 19$

15·0	0·001
14·0	0·031
13·0	0·335
12·0	2·186
11·0	9·057
10·0	25·254

$m = 17,\ n = 20$

15·0	0·001
14·5	0·004
14·0	0·020
13·5	0·063
13·0	0·228
12·5	0·585
12·0	1·585
11·5	3·300
11·0	7·014
10·5	12·121

$m = 17,\ n = 21$

15·0	0·002
14·0	0·042
13·0	0·407
12·0	2·443
11·0	9·568
10·0	25·741

$m = 17,\ n = 22$

15·0	0·001
14·5	0·005
14·0	0·027
13·5	0·079
13·0	0·285
12·5	0·668
12·0	1·816
11·5	3·539
11·0	7·558
10·5	12·471

$m = 17,\ n = 23$

15·0	0·003
14·0	0·053
13·0	0·477
12·0	2·678
11·0	10·014

$m = 17,\ n = 24$

15·0	0·002
14·5	0·007
14·0	0·036
13·5	0·095
13·0	0·342
12·5	0·745
12·0	2·033
11·5	3·751
11·0	8·046
10·5	12·770

$m = 18,\ n = 18$

15·0	0·008
14·0	0·111
13·0	0·920
12·0	4·717
11·0	15·877

$m = 18,\ n = 19$

15·5	0·001
15·0	0·005
14·5	0·019
14·0	0·072
13·5	0·220
13·0	0·635
12·5	1·535
12·0	3·486
11·5	6·828
11·0	12·559

$m = 18,\ n = 20$

16·0	0·001
15·0	0·012
14·0	0·146
13·0	1·085
12·0	5·157
11·0	16·499

$m = 18,\ n = 21$

15·5	0·001
15·0	0·007
14·5	0·025
14·0	0·098
13·5	0·266
13·0	0·772
12·5	1·712
12·0	3·904
11·5	7·193
11·0	13·300

$m = 18,\ n = 22$

16·0	0·001
15·0	0·016
14·0	0·182
13·0	1·242
12·0	5·548
11·0	17·032

$m = 18,\ n = 23$

16·0	0·001
15·5	0·002
15·0	0·011
14·5	0·033
14·0	0·125
13·5	0·311
13·0	0·906
12·5	1·872
12·0	4·288
11·5	7·509
11·0	13·951

$m = 19,\ n = 19$

16·0	0·003
15·0	0·045
14·0	0·428
13·0	2·511
12·0	9·694
11·0	25·856

$m = 19,\ n = 20$

16·0	0·002
15·5	0·007
15·0	0·029
14·5	0·094
14·0	0·290
13·5	0·748
13·0	1·816
12·5	3·800
12·0	7·484
11·5	13·009

$m = 19,\ n = 21$

16·0	0·004
15·0	0·062
14·0	0·519
13·0	2·808
12·0	10·246

$m = 19,$	$n = 22$	$m = 20,$	$n = 20$	$m = 20,$	$n = 21$	
16·0	0·003	17·0	0·001	17·0	0·001	
15·5	0·010	16·0	0·018	16·5	0·003	
15·0	0·041	15·0	0·192	16·0	0·011	
14·5	0·117	14·0	1·282	15·5	0·039	
14·0	0·363	13·0	5·642	15·0	0·129	
13·5	0·854	12·0	17·153	14·5	0·352	
13·0	2·082			14·0	0·910	
12·5	4·078			13·5	2·027	
12·0	8·069			13·0	4·259	
11·5	13·391			12·5	7·888	
				12·0	13·784	

Souhrn

TABULKY PRO DVOUVÝBĚROVÝ MEDIÁNOVÝ TEST

ZBYNĚK ŠIDÁK

Pro neparametrický mediánový test pro dva výběry, jejichž rozsahy m, n splňují $3 \leqq m \leqq n$, $m + n \leqq 41$, se tabelují pravděpodobnosti horních konců rozložení až do bodu, kde je po prvé překročeno 10%.

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